A Wordsearch

Given an N by N wordsearch and N words, devise an algorithm to solve the wordsearch in $O(N^3)$. For simplicity, assume no word is contained within another, i.e. if the word "bear" is given, "be" wouldn't also be given.

If you are unfamiliar with wordsearches or want to gain some wordsearch solving intuition, see below for an example wordsearch. Note that the below wordsearch doesn't follow the precise specification of an N by N wordsearch with N words, but your algorithm should work on this wordsearch regardless.

Example Wordsearch:

С	М	U	н	0	S	А	Е	D		
Т	R	А	т	н	А	Ν	к	А		
0	С	Y	Е	S	R	т	U	Т		
Ν	Т	R	S	А	Т	0	L	S		
Y	R	R	М	т	Ν	Ν	н	R		
Y	Е	А	Е	v	А	R	U	Е	ajay crystal	anton eric
А	А	А	Т	М	Е	L	С	R	grace	isha
Ν	н	D	J	Y	U	А	С	T	luke rica	naama sarina
т	Y	S	А	А	R	S	U	С	sherry	shreyas
А	R	S	T	G	Y	Е	S	А	sohum tony	sumer vidya

Hint: Add the words to a Trie, and you may find the longestPrefixOf operation helpful. Recall that longestPrefixOf accepts a String key and returns the longest prefix of key that exists in the Trie, or **null** if no prefix exists.